

## Self-organization and criticality in ecological systems with antagonistic interactions

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Complex systems are characterized by a large number of components whose interactions are both nonlinear and local. Two main classes of systems are recognized that produce patterns of self-organization, with different implications for sensitivity to external perturbations and for the occurrence of large and unpredictable intermittent fluctuations. These classes correspond to systems that exhibit, respectively, classical phase-transitions [1] and self-organized criticality (SOC,[2, 3]). With two individual-based models that are spatial and stochastic and are implemented as interacting particle systems, we introduce a third class of systems. The first model is for the dynamics of predator and prey [4]; the second, for the dynamics of disturbance and recovery [5]. We show that the models exhibit a percolation-type transition with similarities and differences to static percolation. One important difference is a broader critical region, which we use to explain the origin of robust power-law scalings [6, 7]. At the critical point, these systems exhibit a drastic change in cluster connectedness but not in the biological variables of interest.

Based on these results and on the literature on spatial and individual-based models for predator-prey, disease, and disturbance dynamics, we propose a classification of ecological systems with local antagonistic interactions. We establish the biological and mathematical assumptions that differentiate the three main classes, and discuss the implications of the

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different types of dynamics for patterns of population ‘stability’ and their relationship to spatial connectedness.

## References

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